



# Digital Signal Processing - SS15

## Theory Tutorial 2

### Linear Systems

**PROBLEM ONE** Determine the properties of the following systems in respect of:  
(1) stability, (2) causality, (3) linearity and (4) time invariance. Justify your answers.

(a) 
$$T\{x[n]\} = \sum_{k=n_0}^n x[k]$$

(b) 
$$T\{x[n]\} = \sum_{k=n-n_0}^{n+n_0} x[k]$$

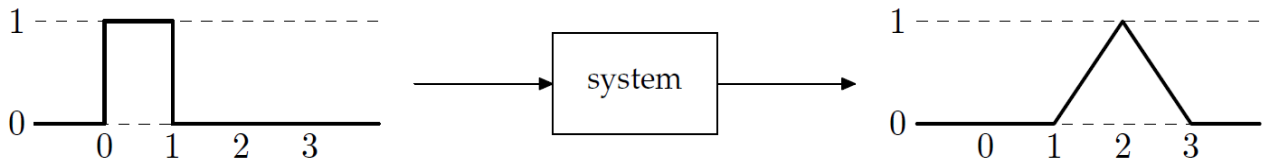
(c) 
$$T\{x[n]\} = x[n-n_0]$$

(d) 
$$T\{x[n]\} = e^{x[n]}$$

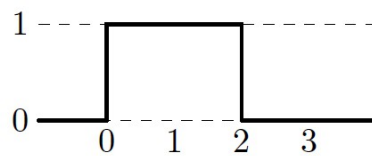
(e) 
$$T\{x[n]\} = ax[n] + b$$

(f) 
$$T\{x[n]\} = x[-n]$$

**PROBLEM TWO** A given linear, time-invariant system turns an unit pulse into a triangle:



The system is given the following input signal:



Sketch the output signal.

## Keys

### P1.

- (a) Unstable, non causal, linear, time-varying.
- (b) stable, non causal, linear, time-invariant.
- (c) stable, causal if  $n_0 \geq 0$ , otherwise non causal, linear, time-invariant.
- (d) stable, causal, non linear, time-invariant.
- (e) stable, causal, non linear, time-invariant.
- (f) stable, non causal, linear, time-varying.

### P2. N.A.